

به نام خدا

طرح درس سیستم‌های کلی جبر

این درس به طور کلی برای دانشجویان مقطع دکتری ریاضی گرایش جبر طراحی و برنامه ریزی شده است.

فصل ها و بخش‌هایی که در این درس ارائه می‌شوند به ترتیب زیر است.

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\$ 1. Free modules

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1B. Stable Finiteness

1C. The Rank Condition

1D. The Strong Rank Condition

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2C. Invertible Fractional Ideals

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2E. Hereditary Artinian Rings

2F. Trace Ideals

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3D. Essential Extensions and Injective Hulls

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3F. Indecomposable Injectives and Uniform Modules

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